



**Damietta University  
Faculty of Commerce  
English Program**

**Production and Operations Management**

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# Location Strategies

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# Location Strategies

## Transportation Models



# Outline

- ▶ Transportation Modeling
- ▶ Developing an Initial Solution
- ▶ The Stepping-Stone Method
- ▶ Special Issues in Modeling



# Special Issues in Modeling

- ▶ Demand not equal to supply
  - ▶ Called an unbalanced problem
  - ▶ Common situation in the real world
  - ▶ Resolved by introducing dummy sources or dummy destinations as necessary with cost coefficients of zero

# Virtual Trial for Dummy Variable

$$\begin{aligned} \text{Total Cost} &= 250(\$5) + 50(\$8) + 200(\$4) + 50(\$3) + 150(\$5) + 150(0) \\ &= \$3,350 \end{aligned}$$

From \ To	(A) Albuquerque	(B) Boston	(C) Cleveland	Dummy	Factory capacity
(D) Des Moines	250 \$5	\$4	\$3	0	250
(E) Evansville	50 \$8	200 \$4	50 \$3	0	300
(F) Fort Lauderdale	\$9	\$7	150 \$5	150 0	300
Warehouse requirement	300	200	200	150	850

New  
Des Moines  
capacity



# Special Issues in Modeling

- ▶ Degeneracy
  - ▶ To use the stepping-stone methodology, the number of occupied squares in any solution must be equal to the number of rows in the table plus the number of columns minus 1
  - ▶ If a solution does not satisfy this rule it is called degenerate

Test of degeneracy in our example:

$$\begin{aligned}\text{Occupied squares} &= (\text{No. Columns} + \text{No. Rows}) - 1 \\ &= 6 - 1 = 5, \text{ *was no degeneracy*}\end{aligned}$$

# What to do if there is Degeneracy?

$$\text{Total Cost} = \$8(100) + \$9(100) + \$9(20) + \$7(80) = \$2,440$$

From \ To	Customer 1	Customer 2	Customer 3	Warehouse supply
Warehouse 1	100   \$8	\$2	\$6	100
Warehouse 2	0   \$10	100   \$9	20   \$9	120
Warehouse 3	\$7	\$10	80   \$7	80
Customer demand	100	100	100	300

Initial solution is degenerate

Place a zero quantity in a **proper** unused square and proceed computing improvement indices

Proper unused cell meets two criteria!!!



# What to do if there is Degeneracy?

From \ To	Customer 1	Customer 2	Customer 3	Warehouse supply
Warehouse 1	100 \$8	\$2	\$6	100
Warehouse 2	0 \$10	100 \$9	20 \$9	120
Warehouse 3	\$7	\$10	80 \$7	80

Customer demand

$$W1C2 \text{ index} = \$2 - \$9 + \$10 - \$8 = -\$5$$

$$W1C3 \text{ index} = \$6 - \$9 + \$10 - \$8 = -\$1$$

$$W3C1 \text{ index} = \$7 - \$7 + \$9 - \$10 = -\$1$$

$$W3C2 \text{ index} = \$10 - \$7 + \$9 - \$9 = +\$3$$

# What to do if there is Degeneracy?

$$\text{Total Cost} = \$2(100) + \$10(100) + \$9(20) + \$7(80) = \$1,940$$

From \ To	Customer 1	Customer 2	Customer 3	Warehouse supply
Warehouse 1	\$8	100 \$2	\$6	100
Warehouse 2	100 \$10	0 \$9	20 \$9	120
Warehouse 3	\$7	\$10	80 \$7	80
Customer demand	100	100	100	300

This solution is also degenerate

Place a zero quantity in a **proper** unused square and proceed computing improvement indices

# What to do if there is Degeneracy?

From \ To	Customer 1	Customer 2	Customer 3	Warehouse supply
Warehouse 1	\$8	100 \$2	\$6	100
Warehouse 2	100 \$10	0 \$9	20 \$9	120
Warehouse 3	\$7	\$10	80 \$7	80

Customer demand

$$W1C1 \text{ index} = \$8 - \$2 + \$9 - \$10 = +\$5$$

$$W1C3 \text{ index} = \$6 - \$9 + \$9 - \$2 = +\$4$$

$$W3C1 \text{ index} = \$7 - \$7 + \$9 - \$10 = -\$1$$

$$W3C2 \text{ index} = \$10 - \$7 + \$9 - \$9 = +\$3$$

# What to do if there is Degeneracy?

$$\text{Total Cost} = \$2(100) + \$10(20) + \$9(100) + \$7(80) = \$1,860$$

From \ To	Customer 1	Customer 2	Customer 3	Warehouse supply
Warehouse 1	\$8	100 \$2	\$6	100
Warehouse 2	20 \$10	0 \$9	100 \$9	120
Warehouse 3	80 \$7	\$10	\$7	80
Customer demand	100	100	100	300

This solution is also degenerate

Place a zero quantity in a **proper** unused square and proceed computing improvement indices

# What to do if there is Degeneracy?

Since all indices are positive, thus, this solution is the optimal solution with a total cost of \$1,860

From \ To	Customer 1	Customer 2	Customer 3	Warehouse supply
Warehouse 1	\$8 100	\$2	\$6	100
Warehouse 2	20 \$10	0 \$9	100 \$9	120
Warehouse 3	80 \$7	\$10	\$7	80
Customer demand				

  

$\text{W1C1 index} = \$8 - \$2 + \$9 - \$10 = +\$5$ $\text{W1C3 index} = \$6 - \$9 + \$9 - \$2 = +\$4$ $\text{W3C2 index} = \$10 - \$7 + \$10 - \$9 = +\$4$ $\text{W3C3 index} = \$7 - \$7 + \$10 - \$9 = +\$1$
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Thank you

