



الدرجة الكلية: 70
زمن الامتحان: ساعتين

امتحان نهاية الفصل الدراسي الثاني
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كلية العلوم
قسم الرياضيات

Answer the following questions:

Question One:

- 1) Compare between the different classes of thermodynamic systems.
- 2) Define the Helmholtz free energy and Enthalpy.
- 3) Calculate both the coefficient of thermal expansion and the coefficient of isothermal compressibility for the ideal gas.

Question Two:

- 1) Write short notes on the uncertainty and degeneracy principles.
- 2) Prove that the number of microstates of the state (N_1, N_2, \dots, N_m) is $w = \frac{N!}{N_1!N_2!\dots N_m!}$
where $N = \sum_{i=1}^m N_i$.

Question Three:

- 1) Study the distribution of microstates of a system consists of three distinguishable particles and has four energy levels $E_i = i\epsilon$, $i = 0, 1, 2, 3$, such that the total energy $U = 3\epsilon$.
- 2) A system consists of 4000 distinguishable particles and has three degenerate energy levels $E_i = i\epsilon$, $i = 0, 1, 2$. The degree of degeneracy is g for all levels. Find the number of particles in each level for the most probable distribution, where the internal energy is 2300ϵ .

Question Four:

- 1) Consider a system has a constant large number of identical and distinguishable particles N . The particles are distributed to the energy levels E_1, E_2, \dots , where the number of particles in the i^{th} energy level is N_i . Derive Maxwell-Boltzmann distribution and compute the average, variance, and standard deviation of energy.
- 2) Consider a system consisting of N distinguishable particles. Each particle can be in one of two microstates with single-particle energy 0 and ϵ . The system is in equilibrium at temperature T . Find the thermodynamic properties of the system.

With my best wishes

Examiner:

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