

**Using MATLAB to solve the following**

(1)

The value of  $\pi$  can be estimated from the expression:

$$\frac{2}{\pi} = \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{2+\sqrt{2}}}{2} \cdot \frac{\sqrt{2+\sqrt{2+\sqrt{2}}}}{2} \cdot \dots$$

Write a MATLAB program in a script file that determine  $\pi$  for any number of terms. The program asks the user to enter the number of terms, and then calculates the corresponding value of  $\pi$ . Execute the program with 5, 10, and 40 terms. Compare the result with `pi`. (Use `format long`.)

(2)

Determine the solution of the following differential equation that satisfies the given initial conditions. Plot the solution for  $0 \leq t \leq 7$ .

$$\frac{d^2y}{dt^2} - 0.08 \frac{dy}{dt} + 0.6t = 0, \quad y(0) = 2, \quad \left. \frac{dy}{dx} \right|_{x=0} = 3$$